Large scale and hybrid computing with CP2K

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Sustainable energy production

A grand challenge for society which will require novel materials engineered with atomistic precision


Novel simulation tools can contribute towards rational design of complex systems
Modeling complex systems


A computationally tractable reference system of non-interacting particles can be used to obtain all properties (in particular the density and energy) of a true electronic system. The required external potential (Vxc) exists but is only known approximately.

\[
\left[-\frac{\hbar^2}{2m} \nabla^2 + V_s(\vec{r})\right] \phi_i(\vec{r}) = \epsilon_i \phi_i(\vec{r})
\]

\[
V_s(\vec{r}) = V(\vec{r}) + \int \frac{e^2 n_s(\vec{r}')}{|\vec{r} - \vec{r}'|} d^3r' + V_{XC}[n_s(\vec{r})]
\]
Modeling complex systems

- **Scale**
  - ~10 atoms
  - ~1-100 ps

- **Multi-scale**
  - ~1,000 atoms
  - ~1-1000 ns

- **Empirical models**
  - ~100,000 atoms
  - ~1-1,000 ns

- **Enhanced sampling**

- **Reduced dimensionality**
  - All timescales
What is CP2K?

CP2K is a freely available program to perform atomistic and molecular simulations of solid state, liquid, molecular and biological systems. It provides a general framework for different methods such as e.g. density functional theory (DFT) [...]
Gaussian and plane waves: GPW in CP2K

\[
\left[-\frac{\hbar^2}{2m} \nabla^2 + V_s(\vec{r})\right] \phi_i(\vec{r}) = \epsilon_i \phi_i(\vec{r})
\]

• **Primary basis:** Gaussians
  - compact
  - sparse $H^{ks}$ (and $P$)
  - Many terms analytic

• **Auxiliary basis:** Plane waves
  - regular grid for electron density
  - FFT for Poisson equation
  - No four center integrals needed

The GPW algorithm: compute the GGA Kohn-Sham matrix in $O(N)$ time, PBC are natural.

CP2K: the swiss army knife of molecular simulation

- A wide variety of models Hamiltonians
  - classical
  - semi-empirical
  - local and non-local DFT
  - Combinations (e.g. QM/MM)
- Various algorithms
  - Molecular dynamics & Monte Carlo
    - NVE, NVT, NPT
  - Free energy and PES tools
  - Ehrenfest MD
- Properties
  - Vibrational
  - NMR, EPR, XAS, TDDFT
- Open source & rapid development
  - 900,000 lines of code
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What is CP2K: team


Ten years of development at 200 lines / day = O(1M) SLOC, with a large base of contributors
How do we collaborate?

- SVN
- Email
- Meet & Talk

An animated view of SVN history
A unified view of ligand-protected gold clusters as superatom complexes

Michael Walter, Jaakko Akola, Olga Lopez-Acevedo, Pablo D. Jadzinsky, Guillermo Calero, Christopher J. Ackerson, Robert L. Whetten, Henrik Grönbeck, and Hannu Häkkinen

PNAS July 8, 2008 vol. 105 no. 27 9157–9162

System size: 762 Atoms
~3400 electrons

Electronic structure of nanoparticles
Large variation of vacancy formation energies in the surface of crystalline ice

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Disordered and frustrated materials
Modular and predictable assembly of porous organic molecular crystals

James T. A. Jones, Tom Hasell, Xiaofeng Wu, John Bacsà, Kim E. Jelfs, Marc Schmidtmann, Samantha V. Chong, Dave J. Adams, Abbie Trewin, Florian Schiffmann, Furio Cora, Ben Slater, Alexander Steiner, Graeme M. Day, and Andrew I. Cooper

Structure prediction of metal organic frameworks
An atomistic picture of the regeneration process in dye sensitized solar cells

Florian Schiffmann\textsuperscript{a}, Joost VandeVondele\textsuperscript{a,\textdagger}, Jürg Hutter\textsuperscript{a}, Atsushi Urakawa\textsuperscript{b}, Ronny Wirz\textsuperscript{b}, and Alfons Baiker\textsuperscript{b}

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4830–4833 | PNAS | March 16, 2010 | vol. 107 | no. 11

Functionalized solid/liquid interfaces
CP2K: algorithms

The power & challenge of CP2K: a wide range of algorithms with good scaling properties

- Regular grids: halo-exchange, 3D FFT, Poisson solver, multigrids
- Dense Linear Algebra: Multiply, Diagonalization, Cholesky, ...
- Sparse Linear Algebra: Matrix Multiply
- Particles: time integration, Monte Carlo sampling
- Chemical: 4 center integrals, HFX, MP2, XC, ...

A single kernel rarely dominates
Scaling is $O(N)...O(N^{**5})$

a) Depending on method and system size various kernels will dominate
b) Depending on the dominating kernel, particular hardware might be suitable
c) If several kernels dominate optimization is more of a challenge
Modern Compute Resources for atomistic simulation

Perform calculations that

+/- complete faster
  - AIMD: at the limit of strong scaling (network)
  + Ensemble simulations: connect to experiment
+ are cheaper
+ are technically better converged (grids, basis, sampling)
+ are based on more accurate theory
+ are based on larger models
For a typical user benchmark, the per node (~ per Watt) performance has improved significantly.
CP2K on CSCS production hardware

Per core, we can fight the clock-frequency trend....
XE6 in the above graph is 32 cores per node.
Complex hardware: NUMA nodes with PCI devices

Should we leave thread placement, Task placement and memory management to the system?
Complex hardware: Network topology

3D Torus on the XK6

'Nearest neighbor comms on a 2D grid'

Need to think about process layout or we need better networks.
Entropy and free energy are absolutely important properties, and required to make contact with experiment. They can be computed by generating ensembles of configurations (dynamics / Monte Carlo)

High throughput computing is the best way to achieve good sampling and converged statistics.
More accurate theory:

From 'GGA' to 'HFX' to 'MP2'
Exchange and correlation functionals of improving can be constructed by adding new ingredients.

Each rung on the ladder improves accuracy, but also increases complexity:

1) GGA: only relies on the electron density and its gradients (semi-local)

2) Hyper-GGA: hybrid functionals, includes density and the single particle orbitals directly in a non-local way through Hartree-Fock exchange (HFX)

3) Double hybrids: include some MP2-like terms

\[ V_s(\vec{r}) = V(\vec{r}) + \int \frac{e^2 n_s(\vec{r}')}{|\vec{r} - \vec{r}'|} \, d^3 r' + V_{XC}[n_s(\vec{r})] \]
Hartree-Fock exchange

\[ E_{x}^{\text{HF}} = -\frac{1}{2} \sum_{\alpha\beta\gamma\delta} P_{\alpha\beta} P_{\gamma\delta} (\phi_{\alpha}\phi_{\gamma}|\phi_{\beta}\phi_{\delta}) \]

\[ (\phi_{\alpha}\phi_{\gamma}|\phi_{\beta}\phi_{\delta}) = \int drdr' \frac{\phi_{\alpha}(r)\phi_{\gamma}(r)\phi_{\beta}(r')\phi_{\delta}(r')}{|r - r'|} \]

An easy term in Gaussian basis sets, but brute force scaling as \( O(N^4) \)

2'825 atoms
→ 31'247 basis functions
→ 976'375'009 elements in \( P \)
→ 953'308'158'199'750'081 integrals

Exa-Pet-Ter-Gig-Meg-Kil

Do we need exa-scale computing, or can we be scientist?
$O(N^4) \rightarrow O(N)$

$$E_x^{\text{HF}} = -\frac{1}{2} \sum_{\alpha\beta\gamma\delta} P_{\alpha\beta} P_{\gamma\delta} (\phi_\alpha \phi_\gamma | \phi_\beta \phi_\delta)$$

$$P_{\alpha\beta} = \int drdr' \frac{\phi_\alpha(r) \phi_\gamma(r) \phi_\beta(r') \phi_\delta(r')}{|r-r'|}$$

Based on the fact that for large systems either the integrals or the density matrix become zero (to within a threshold $\epsilon$)

Cauchy-Schwarz screening $\quad |(ab|cd)| \leq \sqrt{(ab|ab)(cd|cd)} \quad O(N^2)$

Density matrix screening $\quad P_{\alpha\beta}$ decays exponentially $\quad O(N)$

Operator screening $\quad$ Operators other than $1/r \quad O(N)$
Linear scaling is key .... thousands of molecules possible
On 'standard' cluster hardware in minutes.
Parallel implementation: OMP/MPI

\[ E = v^T(Mv) ? \]

Distribute the matrix \( M \) (dim: \( 10^9 \times 10^9 \)), replicate the vector \( v \)

Simple communication pattern (\( v \) is distributed in GGA mode) allows for exploiting the full symmetries (8x speedup)

\[ (ab|cd) = (ba|cd) = (ba|dc) = (ab|dc) = (cd|ab) = (cd|ba) = (dc|ba) = (dc|ab) \]

Advanced load balancing model used

\( v \) and \( (Mv) \) can be rather large vectors (\( 10^9 \) elements)

Exploit current architectures (e.g. 16 cores with 16Gb per node) \( \rightarrow \) MPI/OpenMP

Shared \( v \) and \( (Mv) \), \( v \) is read-only, \( (Mv) \) is atomically updated

Exploit that only \( O(N) \) entries of \( v \) are non-zero \( \rightarrow \) sparse storage for \( v \)

Remaining memory used for storing \( M \).
Many-core era: OMP/MPI

Main benefits:
- Increase memory per MPI task
- Extend the scalability plateau
- Access >10000s of cores
- Interface to GPU (XK6)
- Speedups for some parts of the code

Main issues:
- Loop level OMP is not sufficient
- Analyzing OMP performance difficult
- Non-deterministic threading bugs
- Libraries (scalapack) poorly threaded
- Compilers & tools

Here computer centers can help! EPCC (EPSRC/PRACE funded) did so.
Parallel efficiency

HFX remains computationally much more demanding than GGA DFT (10x?)
A good parallel implementation is mandatory

10 steps of MD, 64 $\text{H}_2\text{O}$, 2560 BF,
OpenMP: 8 threads/node

HFX code out-scales the
Remaining (GGA) part of CP2K

Provided enough compute power,
Hybrid simulations run essentially as fast as GGA
(9s / BOMD step @ 4096 cores)
In-core integral compression

Almost all simulations are performed using an in-core algorithm → 10x speedup is observed.
Highly efficient scheme: index free and lossy compression

Guidon, M; Schiffmann, F; Hutter, J; VandeVondele, J. 2008 ; JCP 128(21): 214104
LiH: Parallel efficiency & in-core operation

Initial speed:
Using CPU efficiently

Superlinear speedups:
Using all memory

Good scale-out:
Using network

Paier J; Diaconu CV; Scuseria GE; Guidon M; VandeVondele J; Hutter J. 2009: PRB 80(17): 174114
Auxiliary Density Matrix Methods (ADMM)

For certain density matrices HFX can be computed very efficiently (e.g. small basis sets or increased sparsity)

Transform an expensive matrix into a cheap one, use a GGA for estimating the difference

\[
E_x^{\text{HFX}}[P] = E_x^{\text{HFX}}[\hat{P}] + (E_x^{\text{HFX}}[P] - E_x^{\text{HFX}}[\hat{P}])
\approx E_x^{\text{HFX}}[\hat{P}] + (E_x^{\text{DFT}}[P] - E_x^{\text{DFT}}[\hat{P}])
\]

One example: wavefunction fitting, using an auxiliary basis

\[
\min_{\hat{c}} \left[ \sum_j \int (\psi_j(\mathbf{r}) - \hat{\psi}_j(\mathbf{r}))^2 d\mathbf{r} + \sum_{k,l} \Lambda_{kl} \left( \int \hat{\psi}_k(\mathbf{r}) \hat{\psi}_l(\mathbf{r}) d\mathbf{r} - \delta_{kl} \right) \right]
\]

Guidon M; Hutter J; VandeVondele J; JCTC 6(8): 2348-2364
ADMM: performance

A fully solvated protein computed within minutes using hybrid functionals

Computer science must be combined with domain knowledge!

Guidon M; Hutter J; VandeVondele J; JCTC 6(8): 2348-2364
Møller-Plesset Perturbation Theory

The energy:

\[ E^{(2)} = - \sum_{i,j,ab}^{occ,vir} (ia|jb)[2(ia|jb) - (ib|ja)] \frac{\varepsilon_a + \varepsilon_b - \varepsilon_i - \varepsilon_j}{\varepsilon_{12}} \]

Two electron integrals over canonical molecular orbitals (MO):

\[ (ia|jb) = \int \int \psi_i(\vec{r}_1) \psi_a(\vec{r}_1) \frac{1}{\vec{r}_{12}} \psi_j(\vec{r}_2) \psi_b(\vec{r}_2) d\vec{r}_1 d\vec{r}_2 \]

The four index transformation, going from AO to MO

\[ (ia|jb) = \sum_{\mu \nu \lambda \sigma} (\mu \nu | \lambda \sigma) C_{\mu i} C_{\nu a} C_{\lambda j} C_{\sigma b} \]

MP2 is relatively expensive \( O(N^5) \), not easy to parallelize efficiently, and somewhat tricky in the condensed phase for an AO code.
GPW-MP2

A Gaussian and plane waves approach to MP2

\[
(i a | \lambda \sigma) = \int \int \psi_i(\vec{r}_1) \psi_a(\vec{r}_1) \frac{1}{\vec{r}_{12}} \phi_\lambda(\vec{r}_2) \phi_\sigma(\vec{r}_2) d\vec{r}_1 d\vec{r}_2
\]

\[
= \int \left[ \int \frac{\psi_i(\vec{r}_1) \psi_a(\vec{r}_1)}{\vec{r}_{12}} d\vec{r}_1 \right] \phi_\lambda(\vec{r}_2) \phi_\sigma(\vec{r}_2) d\vec{r}_2
\]

\[
= \int \left[ \int \frac{\rho^{ia}(\vec{r}_1)}{\vec{r}_{12}} d\vec{r}_1 \right] \phi_\lambda(\vec{r}_2) \phi_\sigma(\vec{r}_2) d\vec{r}_2
\]

\[
= \int v^{\lambda a}(\vec{r}_2) \phi_\lambda(\vec{r}_2) \phi_\sigma(\vec{r}_2) d\vec{r}_2
\]

Directly obtain half transformed integrals using the GPW approach:

Leads to a highly efficient parallel implementation.

Del Ben M, Hutter J, VandeVondele J: to be submitted
Parallel efficiency

CO$_2$ crystal (32 molecules)
cc-QZVP basis (5184 BF)
Canonical GPW-MP2 calculation

MP2 time: 9min.
parallel efficiency: 80%
On 102400 cores
Larger model systems
Traditional approaches to solve the self-consistent field (SCF) equations are $O(N^3)$ limiting system size significantly.

A newly implemented algorithm is $O(N)$, allowing for far larger systems to be studied.
Linear Scaling SCF

New regime: small devices, heterostructures, interfaces, nano-particles, a small virus.

Solvated STMV: 1M

Gate-all-around FET

With Mathieu Luisier

1.5M atoms
Anatase nanocrystal

Caplovicova et al. App. Cat. B, 224, 117
Sign matrix iterations

The density matrix (P) is function of H

\[ P = \frac{1}{2} (I - \text{sign}(S^{-1}H - \mu I))S^{-1}. \]

A simple iterative scheme (Newton-Schultz) gives sign(A):

\[ X_{n+1} = \frac{1}{2} X_n (3I - X_n^2). \]

Using only sparse matrix matrix multiplies (not SPMV!) linear scaling can be obtained

A dedicated sparse matrix multiply library is extremely important
This library is being ported to GPUs
Millions of atoms in the condensed phase

Bulk liquid water. Dashed lines represent ideal linear scaling.

VandeVondele, Borstnik, Hutter, JCTC
Towards $O(1)$: constant walltime with proportional resources

Stringent test:
- Small blocks, large overhead
- Very sparse matrices
- Running with 200 atoms / MPI task

Local multiplies constant (OK!).

Overhead & Communication
- Grows with $\sqrt{N}$
- Needs a replacement for Cannon

Work is underway to replace the Cannon algorithm with something new!
Retain the $\sqrt{N}$ max comm, yield constant comm in the limit.
DBCSR: a sparse matrix library

Distributed Blocked Compressed Sparse Row
Distributed Blocked Cannon Sparse Recursive

Target the application: atoms → Blocks (e.g. 5x5, 13x13, 23x23)
Linear scaling → Sparse
Fully dense → Cannon
Large scale → Distributed
High Performance → Recursive

Cannon style communication on a homogenized matrix for strong scaling
The local multiplication

A two stage process:
- Index building: figure out what to calculate
- Computation: Do the calculations

A cache-oblivious recursive approach

LIBSMM: an autotuned CPU library for small matrix multiplication: 2x faster than optimized blas for applications
An auto-tuned small matrix multiply library

\[ C = C + A \times B \]

- Various 'strange' sizes needed
  - 5x5, 5x13, 13x13 ...
- Hand-optimization
  - too difficult
  - too time-consuming
  - not-flexible enough (new chips)
- Auto-generate a separate library
  - Easy
  - Fast
  - Flexible
  - Now available

Libsmm outperforms optimized blas: 2x-10x

Autogeneration – Autotuning … a powerful approach to performance (Atlas, FFTW, ...
GPU Kernel Description

Compute a batch $C_{ij}$, $A_{ik}$, $B_{kj}$ of small matrix block products (5x5 .. 23x23)
Not too different from batched dgemm ($C_{i}=C_{i}+A_{i}B_{i}$) available in cudablas 4.1

CUBLAS Batched dgemm reaches
Only ~50 Gflops for 23x23

Need to:
1) exploit dependencies
   (data reuse)
2) Better compute kernel

Sort batch on $C_{ij}$ so we have only 2 data read/writes instead of 4.
Hand-optimize a CUDA kernel for size 23x23 (playing with registers / occupation etc)
The GPU port of DBCSR (I)

Not so easy … ran into many issues with tools  
… but received excellent support from Cray/NVIDIA/CP2K team

• Up to 3x performance slowdown in MPI for dynamically linked binaries  
  • Fix: use a (not yet released) Cray patched libudreg.so.0 (?)  
• ran into CCE miscompilation  
  • Fix: compile selected file at -O0  
• problems with (virtual) memory management  
  • Fix: use hugepages  
• A CP2K bug  
  • Fix: add a memcpy.  
• Up to 10X threading performance difference between compilers  
  • Investigating (not crucial for final benchmark)  
• Cuda-memcheck crashes/gave false positives  
  • Ignore after checking carefully  
• Usual tools (valgrind or CP2K internal timing/memory trace) do not work  
  • accept

Not a particularly time efficient procedure…
Not for every developer …
Not without excellent support ….
Open Challenges:

• Only one process per node can connect to GPU.
  Need a functional OMPed code as well

• Work sharing between GPU and CPU not yet optimal.
  Have the CPU also do stacks of multiplications?

• Sending data panels to GPU not yet overlapping with any work
  Could be started as soon as MPI completes. Maybe double buffering

• GPU Kernel optimized for 23x23 matrices (water molecule). We need many sizes.
  Needs an auto-tuning and auto-generating framework for the GPU
  A strategy to deal with smaller blocks.
GPU multiplication benchmark

Benchmark matrix-matrix multiplication with random [0..1] matrix, quasi-realistic fill-in pattern

Hybrid MPI+OpenMP+CUDA Fortran/C code

NREP=6: Matrix dimension N=159,000; 50% occupation

<370Mb of data per node on 256 nodes....

CPU (1xIL, XK6): 38 GFLOPS
CPU (2xIL, XE6): 77 GFLOPS (2.3-2.5 GFLOPs/core)
GPU: 114 GFLOPS (110 – 125 GFLOPs)

Current Kernel performance 170 Gflops.

Estimated Keppler performance: 1.6x speedup on kernel

Performance difference: time in MPI

(data Peter Messmer)
GPU application benchmark

- >400 multiplications for 1 run.
- Additional thresholding in multiplications (less flops for same data)
- This week's results.... subject to change

20736 atoms (6912 water molecules), matrix dim 159000, on 576 nodes XK6, 
~60 matrix multiplications / iter.

XK6 without GPU : 1965s per iteration
XK6 with GPU : 924s per iteration

Speedup 2.12x

MPI performance (bandwidth) appears to be the bottleneck (e.g. 50% slowdown
without custom rank reordering):
- Still need to figure out MPI performance (incl. effectiveness of overlap).
- Is the dynamic linking still an issue ?
- Any interference between GPU+CPU ?
- One Communication thread per node enough ?
Further thoughts and conclusions

Computational atomistic modeling is a lot of fun!

A wide range of algorithms is important for DFT simulations

Implementation, algorithm and theory all have their role to play

Good theories and algorithms require knowledge of the scientific problem being solved

Understanding the hardware is important, but challenging given the rapidly changing field

Hierarchical parallelism will be needed to scale to 1000s of nodes.

GPU/MIC/etc. coding is still challenging, will improve as a wider range of software is ported

Large scientific codes will increasingly benefit from new development methodologies.

The Fortran/MPI combo is still the level you can expect in academia
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You for your attention!